MTH 623/Peszynska/Spring 2012 Worksheet 4. Please show all your work. Use proper mathematical notation.

1. Use Lax-Oleinik solution to find the solution to

 $u_t + uu_x = 0,$ 

with initial data  $u_0(x) = H(x)x^2$ . (Hint: part of the solution is  $\frac{1}{2t^2}(1 + 2xt - \sqrt{1 + 4xt}))$ .