

# Using Protocols and Open-Ended Tasks to Promote Student Mathematical Discourse

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# The Plan...

- OMLI
  - What is OMLI?
  - Discourse
  - What we learned about the “Best Practices” for teaching mathematics - setting the stage for discourse using norms and group roles
- “Protocols” defined, with a few examples
- What makes a task “open-ended?”
- An example task from a Business Calculus class

The background of the slide is an abstract composition of diagonal lines in various shades of blue, ranging from a deep navy blue on the left to a very light, almost white blue on the right. The lines are slightly blurred and overlap, creating a sense of depth and movement.

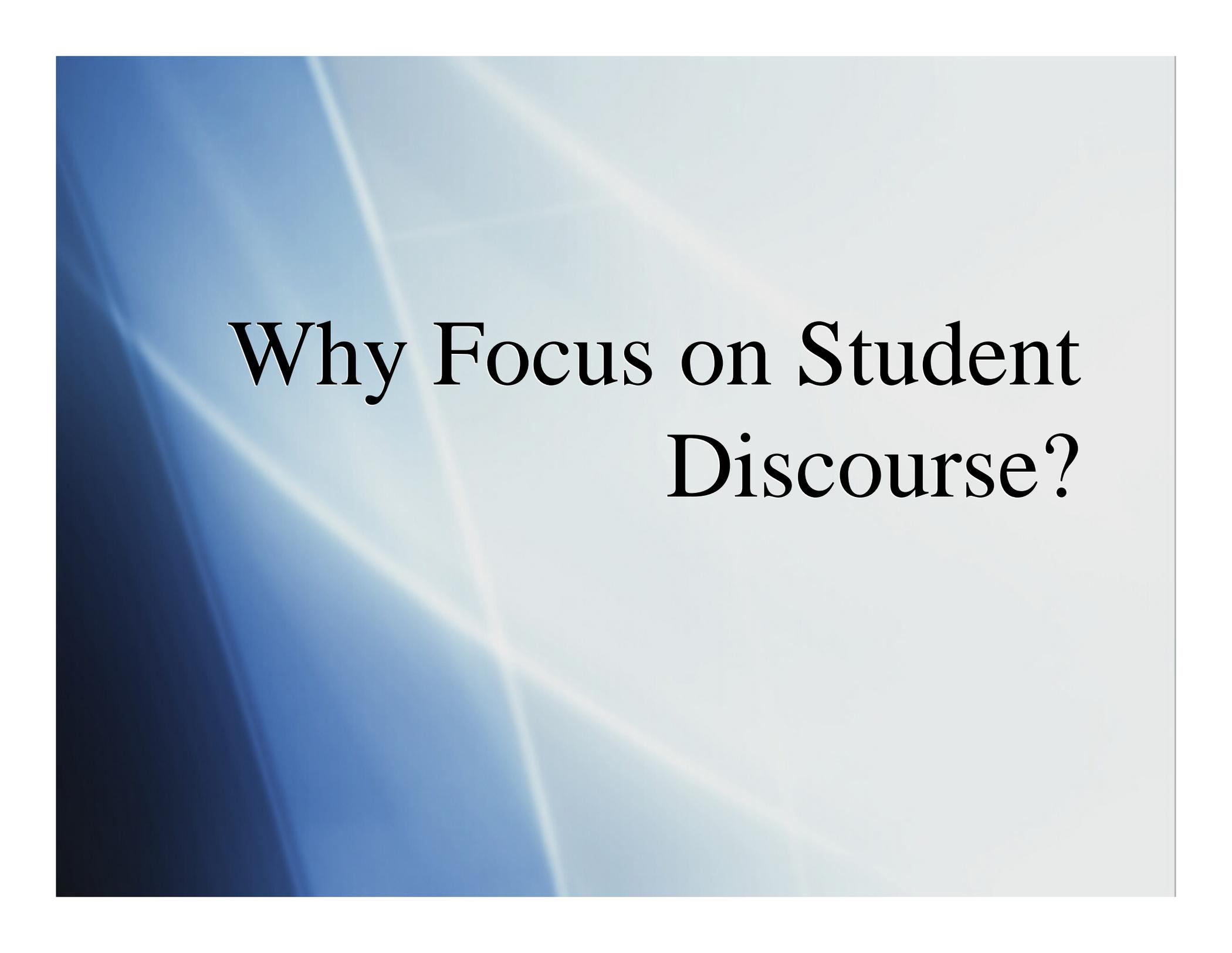
**What is OMILI?**

# Oregon Mathematics Leadership Institute (OMLI)

- NSF-funded partnership project—  
OSU/PSU/TDG/10 OR school districts  
(NSF/EHR-0412553; ODE/Oregon ESEA Title II-B MSP)
- Aimed at increasing mathematics achievement of  
K-12 students
- 3-week intensive summer institutes in 6 different  
mathematics content areas and in leadership skills

# Mathematics Content Courses at OMLI

- 15 two-hour sessions for groups of K–12 teachers with 4-member instructional teams
- Content areas represented:
  - Number and Operation
  - Geometry
  - Abstract Algebra
  - Probability and Statistics
  - Measurement and Change
  - Discrete Mathematics

The background features a gradient from dark blue on the left to light blue on the right, with several bright, curved white lines that create a sense of motion and depth.

# Why Focus on Student Discourse?

In addition to a variety of program evaluation activities, the OMLI evaluation includes a research study component that addresses the following research question: Can student achievement in mathematics be significantly improved by increasing the quantity and quality of meaningful mathematical discourse in mathematics classrooms?"

# Types of Mathematical Discourse

- Explaining
- Questioning
- Challenging
- Relating
- Conjecturing
- Justifying
- Generalizing

# Justification of Mathematical Ideas

- Attention to undefined terms and definitions
- From explanations and generalizations of observed math ideas to answering “why?”
- Oral and written presentation of elementary proofs, from informal to formal

# Pedagogical Lessons from OMLI - What Can We Do to Increase the Quantity & Quality of Discourse Among Students?

- Cooperative groups with student-generated norms for cooperation and assigned group roles
- Use of protocols
- Emphasis on higher-level mathematical discourse
- Hands-on, open-ended explorations

# Group Norms

- Everyone focuses on doing mathematics
- Everyone contributes and shares ideas
- Everyone strives for deep understanding and asks genuine questions
- Everyone tries to create an atmosphere where taking risks is valued
- Everyone helps his or her group-mates to achieve the group task and to adhere to their roles

# Group Roles

- **Team Captain:** responsible for keeping the group on task, for checking in on everyone's progress and understanding
- **Resource Monitor:** responsible for supplying materials and directions from instructor for the entire group

# Group Roles Continued

- Recorder/Reported: responsible for making sure everyone has notes about each activity; sometimes responsible for representing the entire group in group discussions
- Facilitator: responsible for leading the group discussion and keeping everyone participating; in groups of 3 this role doubles up with the team captain

# Protocols

- Pre-determined scenarios of how to complete a task or activity
- Organizational structures of the group process
- Tools for creating an equitable classroom
- Simple (2-step) or very complex ones

# Examples of Protocols

- Think-pair-share
- Private think time followed by a simple go-around protocol
- Go-around and share more ideas each time protocol
- Whole group discussion protocols
- Jigsaw puzzle protocols

# Facilitation of Higher Level Math Discourse

- Use a group-work protocol to ensure everyone takes part in all types of discourse
- Require justifying and conjecturing as a part of task-setting
- Use a whole-group discussion protocol to wrap up group work; for example, ensure ideas flow from concrete to more abstract

# Open-Ended Tasks

- Allow for a variety of approaches or answers
- Make it possible for everyone to be successful
- Generate exciting classroom discussions
- Very effective in the context of protocol-driven facilitation

# Graph Sorting Task

- Originally used in a calculus class for Business and Social Science majors with the purpose of reviewing previously-introduced material for the midterm
- Could also be used as an introductory/motivating task, an informal assessment, or in a variety of other ways

# Private **Think** Time

(5 minutes - then be ready to share with a partner)

1. Sort the graphs (A)-(G) according to some common characteristic of your choosing (be sure you are able to give *mathematical reasons* for putting particular graphs together in the same category.)
2. Then decide how the graphs you grouped together are *different* from one another.

# Pair Up

(10 minutes)

1. Partner #1: Share your graph categories with your partner, giving reasons to support your ideas. Also tell what differences you noticed among the graphs in the same category. Partner #2 listens carefully to Partner #1's ideas during this time.
2. Partner #2: After Partner #1 has shared, ask any clarifying questions needed to understand the thinking and reasoning of your partner.
3. Repeat steps (1) and (2) above with partners switching roles.

# Share Out in Whole-class Discussion

- The whole-class discussion protocol you use next will depend on:
  - The learning goals you have set for the task
  - The ideas generated by the students
  - The time you have allotted for the task
- Private think time: write down two or three ideas for how you might proceed with this task
- In a few minutes, we'll ask you to share your ideas (using a protocol!)

# Wrap up

- As you worked on this task, using the structure of a protocol, what did you notice?
- What questions do you have about discourse, protocols, open-ended tasks, or anything else?